Random Forests of Very Fast Decision Trees on GPU for Mining Evolving Big Data Streams

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Abstract. Random Forests is a classical ensemble method used to improve the performance of single tree classifiers. It is able to obtain superior performance by increasing the diversity of the single classifiers. However, in the more challenging context of evolving data streams, the classifier has also to be adaptive and work under very strict constraints of space and time. Furthermore, the computational load of using a large number of classifiers can make its application extremely expensive.

In this work, we present a method for building Random Forests that use Very Fast Decision Trees for data streams on GPUs. We show how this method can benefit from the massive parallel architecture of GPUs, which are becoming an efficient hardware alternative to large clusters of computers. Moreover, our algorithm minimizes the communication between CPU and GPU by building the trees directly inside the GPU. We run an empirical evaluation and compare our method to two well know machine learning frameworks, VFML and MOA. Random Forests on the GPU are at least 300x faster while maintaining a similar accuracy.

1 INTRODUCTION

Data has become predominant in our modern information society, so much that people often describe it as “the new oil”1. However, data without a model to understand it is just noise. The large amount of data available poses new challenges to computational methods that try to extract knowledge and models from data. In particular, in this work we focus on the challenges in analyzing big data streams.

There is the increasing need for more computational power to process large amounts of data in near real-time. The need to scale data analysis to ever growing big data streams motivates exploring different possible routes, both algorithmic and architectural. In this paper, we explore the usage of Graphics Processing Units (GPUs) to applications of data stream mining.

Recently, GPUs moved from a simple role of 3D accelerators to a more general purpose of mathematical co-processors (GPGPU, General Purpose Graphics Processing Unit). A GPU provides a massively parallel architecture with many cores (up to 2880 cores in most recent model2) and is throughput oriented. Additionally, GPUs have better performance-per-watt than CPUs; it is not a coincidence the top 10 entries of the Green500 all use GPUs.

With the raise of GPUs as a general purpose platform that provides high throughput computation, researchers have started to explore their use in high performance data mining. Deep Learning is an example of a hugely successful application of GPUs to large scale batch learning3. Therefore, it is interesting and challenging to see whether and how we can draw benefits from such an architecture in a streaming context.

In this work, we focus on one of the most common data mining applications: classification. In particular, we study how to effectively deploy decision trees and random forests for data streams on GPUs. These models are very popular in machine learning, but perhaps surprisingly, to the best of our knowledge their streaming deployment on GPUs has not been studied in the literature.

The paper is structured as follows. We present related work in Section 2, our GPU Very Fast Decision Tree in Section 3, and GPU Random Forest for evolving streams in Section 4. In Section 5, we report on their empirical evaluation, and finally we draw conclusions in Section 6.

2 RELATED WORK

The Very Fast Decision Tree or Hoeffding Tree4 is the current state-of-the-art method for building decision trees on data streams. This decision tree method uses a tree as the main data structure. Most of the literature related to using trees on GPUs uses a pre-processing step on the CPU to build the data structure, and then it transfers this data structure to the GPU for parallel traversing. Trees such as k-d trees and octrees are generally used to perform space partitioning in scene rendering and ray tracing. Finally, these trees are usually close to balanced, while decision trees can be very unbalanced.

For example, 6, 8 use a GPU to accelerate the traversing of a k-d tree pre-built on a CPU. The authors of 14 introduce a GPU version of the octree fast enough to allow interactive surface deformation. A novel method for traversing k-d trees for ray tracing is presented in 13. Their method is able to reach peaks of 16 million rays per second with reasonably complex scenes by dividing the tree into smaller trees.

More recent work focuses on building trees directly on the GPU by using parallel construction algorithms. The authors of 11 introduce an in-place method for constructing radix-trees in parallel. This radix-tree is used later as a building block to construct octrees and k-d trees. The main issue with building trees in parallel is that they are a recursive data structure. This fact introduces a challenge as trees are designed to be built sequentially, i.e., you need to build the parent node before building the child node. Furthermore, trees are not linear so it is hard to divide its construction in independent unit of works and later combine their result.

All these works rely on a very regular, predictable, and input-independent structure of the application to design their algorithms.
A very recent new line of research is focusing on applying general transformations. For example, the authors of [7] propose new techniques ("autoropes" and "lockstepping") to traverse irregular trees.

### 3 VERY FAST DECISION TREES ON GPUs

In this section we present GVFDT, our implementation of the VFDT on the GPU. We assume the reader is already familiar with decision tree algorithms and with the VFDT.

An analysis of the VFDT reveals the algorithm has 3 basic phases:

1. **Learning phase.** This phase includes tree traversal in order to find the correct leaf node, class computation and increment of counters for label-attribute-value triplets.
2. **Heuristic computation (e.g., entropy or information gain)** for each attribute at each leaf node.
3. **Model growth**, if needed. This phase executes if the delta between the heuristic of the two best attributes is above a threshold. During this phase, a leaf node is split into two new leaf nodes.

Before explaining the parallel design for these phases, we proceed to define a suitable data structure layout for the tree, as it is the basis for the algorithm and also a very important design decision.

#### 3.1 Tree Layout

The tree is the main data structure used by the GVFDT. Tree traversal is the main operation, as it is performed at both learning and prediction time. The main challenge is that tree traversal is inherently sequential: one needs to know the decision at the parent node in order to get to the correct child. However, GPUs perform poorly on latency-sensitive operations. In order to hide latency, GPU programs run a large number of threads in parallel, so to maximize throughput. Therefore, the tree layout needs to allow for having a large number of threads traversing the tree at the same time.

For simplicity, we only consider binary attributes in the layout, as in the original decision tree algorithm. Therefore, in this case the decision tree becomes a binary tree. This choice lets us use a simple regular data structure to represent the tree: an array. Our tree structure is based in the one in [10]. It uses a breadth-first traversal to encode the binary tree in a single array, level by level. Hence, we can use a basic binary tree search algorithm to traverse the tree. An example of the encoding for a tree with two attributes in depicted Figure 1.

![GVFDT tree encoding](image)

**Figure 1**: GVFDT tree encoding

Each tree node is encoded as a 32-bit unsigned integer that contains an id of 31 bits and a one bit flag. This number corresponds to the maximum number of execution blocks available on the X axis in the GPU ($2^{16}$ for Z and Y axis). The meaning of this id depends on the flag value: if the flag is 1, the node is a leaf and the id is a leaf id, if the flag is 0 the node is an internal node and the id represents an attribute id. With this layout it is easy to obtain the child offset of the child nodes of any given node. Given a node at offset $i$, its left child will be at offset $2i + 1$ and its right child will be at offset $2i + 2$.

GVFDT allocates the memory for the full tree. This very simple design favors speed over space. As we will see in Section 3.3 this can easily become the bottleneck of the algorithm as the tree grows. In this study we resort to ensembles as detailed in Section 4 to sidestep the problem. A memory-efficient tree implementation on GPUs requires a more sophisticated design, which we defer to further studies.

#### 3.2 Tree Leaves

Figure 2 illustrates the two supporting arrays for the GVFDT. The first one is the "leaf class", which stores the class for a given leaf. The second one, "leaf back", is used as a reverse pointer to map a leaf id to an offset in the tree array. We use the latter map when managing the counters and checking if the tree needs to be grown.

The id at each leaf node is used as an offset in the leaf class array in order to get the leaf class label and the corresponding counters. This design decouples the tree representation from actual leaves and counters. In addition, we can reuse leaf ids when splitting the tree and thus keep the supporting arrays compact and fully utilized.

All relevant information is stored at leaves rather than internal nodes. Hence, the tree is just a routing data structure whose only purpose is to reach to a leaf id given a data instance. Keeping separated data structures to store counters and class labels allow us to decouple them from the tree structure. Therefore, we can compute the majority class of a leaf and its split heuristic independently and in parallel.

Finally, when splitting a leaf node, the only extra information we need is a way to go back to the tree offset given its leaf id. The leaf back array serves exactly this purpose. If the algorithm decides to split a node, it replaces the leaf node by an internal node and adds two leaf nodes. However, we only need to allocate one new leaf node as we can reuse the previous leaf node id.

#### 3.3 Learning Phase

This first phase can be divided in 3 smaller steps: 1) tree traversal, 2) counter increase, and 3) class computation.

Traversing the tree means finding the leaf id corresponding to the instance being processed. This step is illustrated in Figure 3. To traverse the tree, a 1D reference system is used inside the block. A thread is assigned to one instance using the y-axis. Using a separate kernel for the tree traversal it is easier as we can force all work to be done together. This may be not enough to completely hide latency but it will help, and hopefully we can benefit from some cache effects.
The output to this step is a vector with as many positions as instances, each containing the class for the instance at that position. Figure 3 shows the 2D leaf-counter layout with four rows used by GVFDT. Each leaf counter is represented by a block inside the grid. In row 0 we store the total number of times value \( n_{ij} \) appeared, rows 2 and 3 store partial counters \( n_{ij} \) for each class \( k \). Row 1 is a mask that keeps track of which attributes have been already used in internal nodes along the path to this leaf node. This binary mask avoids the need for an explicit check on the tree.

For efficiency, rather than computing the heuristic for model growth for each instance, the algorithm does so only every \( \frac{\text{instances}}{\text{min}} \) instances. Therefore, the algorithm can increase a large number of counters in parallel at the same time. Increasing the counters can be highly parallel as each value is totally independent from the others. At first glance this step may seem embarrassingly parallel. However, there might be overlap between the set of counters increased by different thread. Therefore some kind of synchronization is needed. We resort to a parallel reduction approach for this step.

### 3.4 Heuristic: Information Gain

We choose to parallelize the information gain in GVFDT using 2 parallel reductions. Figure 4 illustrates how these reductions work. The first reduction step, in red, is where each thread calculates all the inner \( I_{ij} \) using atomic additions. The second reduction step, in yellow, is done in a similar way where threads now combine each \( I_{ij} \) to obtain the final \( I_i \) for each attribute.

This phase uses a 1D grid layout, mapping each leaf-counter to one block on using the x-axis, to calculate all counters at the same time, no matter if it has been allocated or not for a leaf.

Inside each block we only need one dimension for each possible attribute value. As all attributes are binary, a block needs as much threads as twice the number of attributes and it uses the x-axis only as reference. We do not need a 2D reference per counter, as one thread uses the whole column. In Figure 4 the red step illustrates how each thread only uses the \( a_{ij} \) (rows 2 and 3) and the \( a_{ij} \) (row 0) values on the same column.

The GPU works on all counters at the same time and the way it has to enable or disable attributes without branching is to use the row 1 as an and mask. Each thread will use this mask on the values for its columns, to keep the same value or zero it. There are two risky situations the algorithm needs to care about: a division by zero and the \( \log_2 0 \). CUDA compiler can use a fast floating point operations, or the standard IEEE-754 floating point operation (the one we are using). According the the standard, a division by zero will return a \( \text{NaN} \) (Not A Number). The same way according the NVIDIA log man page, a \( \log_2 0 \) will return \( -\infty \), or \( \text{NaN} \) if \( x < 0 \).

To avoid an explicit check on these values we decided to use the ISA PTX instruction \( \text{max.f32} \), which according the the documentation receives two parameters and if one of them is a \( \text{NaN} \) the instruction will return the other value. We implemented this instruction using an inline assemble functions called and call it in this way \( \text{ptx}_0 \max(0.0, w) \), where \( w \) is the value we want to keep or transform it to 0.

One modification we did in the red step is instead of calculate each \( I_{ij} \) and then multiply it by \( \frac{n_{ij}}{n_{ij}} \), the algorithm do this multiplication while calculating each \( I_{ij} \). As it has already accessed these values to calculate all \( I_{ij} \) it will not cost much but it simplifies the next step (the yellow one in Figure 5).

The second reduction is a simple parallel reduction of sums. The easy way of doing this is with atomic additions using an inverse map to map a counter offset to an attribute. That is, the offsets 0 and 1 (counter position 0 and 1) will be mapped to 0 (attribute 0), and so on.

The output to this kernel is a vector with the attributes information gain values for all leaves, including the unused ones.

### 3.5 Node Split

The node split is the third phase we identified in Section 3. After the heuristic calculation, the algorithm needs to decide if it is time to split or not a leaf. This phase takes as input a vector with the attribute information gain for all leaves.

The layout for the grid in this phase is the same as the explained for the heuristic calculations. The algorithm uses one block per leaf and does the check for all leaf-counters at the same time.

At each block, the kernel first bring all attributes to shared memory to later perform a parallel sort with a little variation. While sorting it uses two vectors: one for the value and the other with the attribute id for the value at the same position. Each time the sorting needs to switch two values it does the switching for on both vectors.

Once the sorting is completed, we know the two best attributes are at positions 0 and 1 on both vectors. And then using the Hoeffding bound the algorithm can decide if the node needs to be split or not. This last check is executed only by thread 0 at each block.
This binomial distribution for large values of

2D planes that use the z coordinate as the tree id. GVFDT lives inside a 2D plane. They can be seen as

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to use the z-axis. Each single GVFDT uses a 1D or 2D grid layout,
tion to aggregate them and pick the most frequent one.
ensemble combines all these votes by using a simple parallel reduc-
to use its y-axis coordinate to obtain the value on this new vector.
traversal, as in this step we only use one thread per instance. We use
increasing counters, we perform this operation right after the tree
same instance by using the same weight. Rather than doing it while
in one position per leaf. Each tree has its own space
attributes each. Each tree has its own space (blue clouds) and is built independently from the other trees.
Our adaptive implementation uses GVFDT as a base learner, on-line bagging [12] to sample instances for each tree, and ADWIN [11] to detect changes in the accuracy of the ensemble members, so that
trees that decrease in accuracy can be replaced with new ones.
In batch mode, bagging builds a set of $M$ base models, training
each model with a bootstrap sample of size $N$ created by drawing random samples with replacement from the original training set. The
training set for each base model contains each of the original training
example $K$ times where $P(K = k)$ follows a binomial distribution.
This binomial distribution for large values of $N$ tends to a Poisson(1)
distribution, where Poisson(1)$= \exp(-1)/k!$. We use this approach
to give each example a weight according to Poisson(1).
In our implementation we need to update all attributes of the
same instance by using the same weight. Rather than doing it while
increasing counters, we perform this operation right after the tree
traversal, as in this step we only use one thread per instance. We use
an extra vector for each instance and tree to store the random Poisson
weight. Hence, when increasing the counters each thread only needs to
use its y-axis coordinate to obtain the value on this new vector.
Finally, each tree gives a prediction vote for each class label. The
ensemble combines all these votes by using a simple parallel reduc-
tion to aggregate them and pick the most frequent one.
To implement the ensemble on the GPU, we extend the grid layout
to use the z-axis. Each single GVFDT uses a 1D or 2D grid layout,
with 1D or 2D components inside the blocks. In turn, each single
GVFDT lives inside a 2D plane. They can be seen as $M$ independent
2D planes that use the z coordinate as the tree id.

4 RANDOM FORESTS ON GPUS

Breiman [3] proposed Random Forests as a method to use random-
ization on the input and on the internal construction of the decision
trees. Random Forests are ensembles of trees with the following char-
acteristics: the input training set is obtained by sampling with re-
placement, the nodes of the tree only may use a fixed number of random
attributes to split, and the trees are grown without pruning.
We use the square root of the total number of attributes as the
number of random attributes to split, as proposed by Breiman. Figure
shows an example of instances with 10 attributes, where each tree
node is using $\sqrt{10} \approx 3$ attributes each. Each tree has its own space
(blue clouds) and is built independently from the other trees.
Our adaptive implementation uses GVFDT as a base learner, on-
line bagging [12] to sample instances for each tree, and ADWIN [11]
to detect changes in the accuracy of the ensemble members, so that
trees that decrease in accuracy can be replaced with new ones.

5 EXPERIMENTAL EVALUATION

We compare GVFDT and GPU Random Forests to similar methods
available in MOA [2] and VFML [9]. MOA is a data stream frame-
work developed in Java at the University of Waikato, New Zealand.
It consists of state-of-the-art algorithms for streaming classification,
regression, clustering, and change detection. VFML is a toolkit in
C for mining evolving data streams developed at the University of
Washington, US.
Both MOA and VFML were used on a system with Intel
Core2Duo E6000 @ 2.4GHz. We run the GPU experiments on a
computer provided by BSC/UPC CUDA Center of Excellence[11] with
the following configuration: 2x Dual-Core AMD Opteron Processor
2223, 8GB RAM, Debian Linux OS, Kernel 3.12-1-amd64 SMP, CUDA compilation tools v5.5.0, and NVIDIA Tesla C2050.
We use three datasets to evaluate our design:
1. The Covertype Dataset has 581,012 instances with 55 attributes
and seven different classes. We use only the 45 of these attributes
that are binary.
2. The Record Linkage Comparison Patterns Dataset (REC) original-
ly has 5,749,132 instances with 9 attributes and 2 classes. In
this dataset, two of the nine attributes have continuous values. We
convert them to binary attributes by computing their quartiles and
encoding the values according to their quartile range.
3. RandomTree (RT) generates 1,000,000 instances with 10 binary
attributes, 2 classes, 5 levels and 20% of noise. This dataset is cre-
ated with the original VFDT data stream generator [5] that pro-
duces concepts that should favor decision tree learners.

5.1 Accuracy Evaluation

We use two metrics for measuring the evaluation performance: ac-
curacy and speed. Accuracy refers to the number of correctly clas-
sified instances divided by the total number of instances used in the

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7.png}
\caption{Counters for all tree in the ensemble.}
\end{figure}

In GVFDT despite using 2D reference systems, all data structures
are single arrays, and kernels use an offset to the position inside the
array. Rather than making $M$ copies of these data structures, we just
make these arrays large enough to hold data for $M$ trees. Thus, we
can easily adapt the GVFDT to run on an ensemble of $M$ trees. In
Figure[7] we show how counters are extended to be used in ensembles.
GVFDT kernels receives as parameters the pointers to the start of
each data structure the kernel needs. In ensembles, we introduce an
intermediate step were each kernel uses the grid z coordinate to get
the offset to the beginning of its data structure. GVFDT kernels can
be called without further modifications.

\textbf{Figure 6:} Ensemble of 100 trees with random attributes.

The decision if a split is needed or not is saved using a vector
which has one position per leaf. Each of this positions are encoded
following the same way as in Figure[1]. Here if the flag is 1 it means
the node needs to be split and the id refers to the attribute id where
to split, otherwise no split is needed and we can ignore the id.
evaluation. Speed refers to the time the model needs to process all instances from a dataset. We use prequential evaluation to measure the model accuracy over time. The prequential evaluation uses each instance first to test the model, and then to train it. With the information obtained from testing, we plot a learning curve to observe how the model evolves over time.

5.1 Single Tree Accuracy Comparison

First, we compare GVDT with the single decision trees in VFML and MOA. A summary of the results are in Table 1. We were not able to evaluate GVDT using the Covertype Dataset, as we could not allocate 2^45 unsigned integer positions for the entire tree. For the Record Linkage Comparison Patterns Dataset (REC) MOA obtains the best result with an accuracy of 99.62%, followed by VFML and GVDT. However, the differences are very small. Also on the RT synthetic dataset, the three decision trees also get very similar performances: VFML obtained (69.03%) followed by MOA with (68.82%) and GVDT close to it (68.41%).

<table>
<thead>
<tr>
<th>Dataset</th>
<th># Instances</th>
<th># att.</th>
<th>VFML</th>
<th>MOA</th>
<th>GVDT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Covertype</td>
<td>5,810,12</td>
<td>45</td>
<td>99.59</td>
<td>76.34</td>
<td>-</td>
</tr>
<tr>
<td>RT</td>
<td>1,000,000</td>
<td>10</td>
<td>69.03</td>
<td>68.82</td>
<td>68.41</td>
</tr>
</tbody>
</table>

5.2 Speed Evaluation

We perform a speed test to compare the new GPU methods with the CPU ones. The setting for these tests is the same as within accuracy, using the prequential learning for MOA, VFML, and GVDT. We first compare single tree speeds, and then Random Forest speeds.

5.2.1 Single Tree Speed Evaluation

Table 3 shows the speed test results for single trees. The surprising results in this table is the performance of VFML compared to MOA: it takes about 15 minutes to process the REC dataset, and about 7 minutes to process the RT dataset. As expected, GVDT performs better than MOA and VFML with an speedup of 22x for the REC dataset, and 25x for the RT dataset. As in Section 5.1.1, we could not test the Covertype dataset for a single tree due to the limitations in our design regarding memory requirements.

<table>
<thead>
<tr>
<th>Dataset</th>
<th># Instances</th>
<th># att.</th>
<th>VFML</th>
<th>MOA</th>
<th>GVDT</th>
<th>Speedup</th>
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<tr>
<td>Covertype</td>
<td>5,810,12</td>
<td>45</td>
<td>107 s</td>
<td>8.2 s</td>
<td>-</td>
<td>22x</td>
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<tr>
<td>REC</td>
<td>5,747,330</td>
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<td>902 s</td>
<td>21.9 s</td>
<td>.98 s</td>
<td>22x</td>
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<tr>
<td>RT</td>
<td>1,000,000</td>
<td>10</td>
<td>422 s</td>
<td>6.5 s</td>
<td>.25 s</td>
<td>25x</td>
</tr>
</tbody>
</table>

5.2.2 Random Forest Speed Evaluation

Results for 100 random tree ensemble tests can be found in Table 4. We can see that GPU Random Forests clearly outperforms MOA for
In this test, 100 random trees run on the GPU at the same time, thus generating more threads for the GPU to schedule. The higher the number of threads available to run contemporarily on the GPU, the better its latency gets hidden. Compared to a single GVFDT tree, ensembles require 2-5 times more time, but obtain higher accuracy.

Figure 11 shows how MOA and GPU Random Forests scale with the number of instances of the REC dataset. In this dataset MOA scales linearly while GPU Random Forests seems to scale almost constantly. This is an effect of the scale, as GPU Random Forests runs in milliseconds instead of minutes. In summary, we can appreciate that GPU Random Forests performs much better than MOA Random Forests for all three datasets.

6 CONCLUSIONS

In this paper we presented efficient streaming Very Fast Decision Trees and Random Forests algorithms designed for the GPU. We started by identifying the phases of execution of the decision tree algorithm, extended them horizontally to increase parallelism, and studied how each of them could be implemented on the GPU. Our streaming Random Forest algorithm uses a per-tree adaptive mechanism to detect changes on the stream so it can react to it. These new methods minimize the communication between the GPU and the CPU to the point that they only need to communicate when the CPU has new instances to process and when the GPU sends the results back to the CPU. We showed how using our adaptive streaming Random Forest on GPUs, speed increases at least 300x. This huge improvement in speed using GPUs opens new challenging possibilities on streaming machine learning for future research.

REFERENCES